

**CHAPTER = 15****MOLECULAR THEORY OF GASES****BOOK NUMERICAL**

- 1 Convert the freezing point of mercury  $-39^{\circ}\text{C}$  into  $^{\circ}\text{F}$  and the comfort level temperature of  $20^{\circ}$  into Kelvin.

**DATA**

$$T_{^{\circ}\text{C}} = -39^{\circ}\text{C}$$

$$T_{^{\circ}\text{F}} = ?$$

$$T_{^{\circ}\text{C}} = 20^{\circ}\text{C}$$

$$T_k = ?$$

**SOLUTIONS**

Celsius to kelvin

$$T_k = T_{^{\circ}\text{C}} + 273$$

$$T_k = 20 + 273 = 293\text{ K}$$

Celsius to Fahrenheit

$$T_{^{\circ}\text{F}} = \frac{9}{5} \times T_{^{\circ}\text{C}} + 32$$

$$T_{^{\circ}\text{F}} = \frac{9}{5} \times (-39) + 32$$

$$T_{^{\circ}\text{F}} = -72.2 + 32$$

$$T_{^{\circ}\text{F}} = -38.2^{\circ}\text{F}$$

- 2 The boiling point of liquid nitrogen is  $-321^{\circ}\text{F}$ . Change it into equivalent kelvin temperature.

**DATA**

$$^{\circ}\text{F} = -321^{\circ}\text{F}$$

$$T_k = ?$$

**SOLUTIONS**

Celsius to kelvin

$$T_k = T_{^{\circ}\text{C}} + 273$$

$$T_k = 20 + 273 = 293\text{ K}$$

**SOLUTIONS**

Fahrenheit to kelvin

$$T_K = \frac{5}{9} (T_{^{\circ}\text{F}} + 459.67)$$

$$T_K = \frac{5}{9} (-321 + 459.67)$$

$$T_K = \frac{5}{9} (138.67)$$

$$T_K = 77\text{ K}$$

- 3 Calculate the volume occupied by a gram-mole of a gas at 0 °C and a pressure of 1.0 atmosphere.

DATA	SOLUTIONS
$T = 0\text{ }^{\circ}\text{C}$	$PV = nRT$
$T = 0 + 273 = 273\text{ K}$	$V = \frac{nRT}{p}$
$P = 1\text{ atm}$	$V = \frac{(1)(0.0821)(273)}{1}$
number of mole $n = 1$	$V = 22.41\text{ liter/mol}$
$R = 0.0821 \frac{\text{L atm}}{\text{mol K}}$	
$V = ?$	

- 4 An air storage tank whose volume is 112 liters contains 3 kg of air at a pressure of 18 atmospheres. How much air would have to be forced into the tank to increase the pressure to 21 atmosphere, assuming no change in temperature

DATA	SOLUTIONS
$V_1 = 112\text{ litres}$	$\frac{P_1 V_1}{m_1} = \frac{P_2 V_2}{m_2}$
$P_1 = 18\text{ atm}$	$\frac{18 \times \cancel{V}}{3} = \frac{21 \times \cancel{V}}{m_2}$
$m_1 = 3\text{ kg}$	$\frac{18}{3} = \frac{21}{m_2}$
$P_2 = 21\text{ atm}$	$m_2 = \frac{3 \times 21}{18}$
$V_1 = V_2 = V$	$m_2 = 3.5\text{ kg}$
$m_2 = ?$	Required of air forced into the tank
	$m = m_2 - m_1$
	$m = 3.5 - 3 = 0.5\text{ kg}$

- 5 A balloon contain  $0.04 \text{ m}^3$  of air at pressure of  $120 \text{ KPa}$ . Calculating the pressure required to reduce its volume to  $0.025 \text{ m}^3$  at constant temperature

**DATA**

$$V_1 = 0.04 \text{ m}^3$$

$$P_1 = 120 \text{ KPa} = 120 \times 10^3 \text{ Pa}$$

$$P_1 = 1.20 \times 10^5 \text{ Pa}$$

$$P_2 = ?$$

$$V_2 = 0.025 \text{ m}^3$$

**SOLUTIONS**

$$P_1 V_1 = P_2 V_2$$

$$(1.20 \times 10^5) (0.04) = P_2 (0.025)$$

$$4800 = P_2 (0.025)$$

$$\frac{4800}{0.025} = P_2$$

$$P_2 = 192000$$

$$P_2 = 1.92 \times 10^5 \text{ Pa}$$

- 6 The molar mass of nitrogen is  $28 \text{ g mol}^{-1}$ . For  $100 \text{ g}$  of nitrogen, calculate.  
 (a) the number of moles.  
 (b) the volume occupied at room temperature ( $20^\circ\text{C}$ ) and pressure of  $1.01 \times 10^5 \text{ Pa}$

**(a)**

The atomic mass of nitrogen (N) is approximately  $14 \text{ g/mol}$ .

the molar mass of nitrogen gas ( $\text{N}_2$ ) is

$$m = 2 \times 14 = 28 \text{ g/mol}$$

$$\text{Number of moles} = \frac{\text{mass in gram}}{\text{molar mass (g/mol)}}$$

$$n = \frac{100}{28} = 3.57 \text{ mol}$$

**(b) DATA**

$$T = 20^\circ\text{C} = 20 + 273 = 293 \text{ K}$$

$$P = 1.01 \times 10^5 \text{ Pa}$$

**SOLUTION**

$$P V = n R T$$

$$V = \frac{n R T}{P}$$

$$V = \frac{(3.57) (8.313) (293)}{1.01 \times 10^5}$$

$$V = 0.086 \text{ m}^3$$

- 7 A sample of gas contains  $3.0 \times 10^{24}$  atoms. Calculate the volume of the gas at a temperature of 300K and a pressure of 120K Pa

**DATA**

$$N = 3.0 \times 10^{24} \text{ atoms}$$

$$N_A = 6.02 \times 10^{23} \text{ atoms}$$

$$n = ?$$

$$T = 300 \text{ K}$$

$$P = 120 \text{ kPa} = 120 \times 1000 \text{ Pa}$$

$$P = 1.20 \times 10^5 \text{ Pa}$$

**SOLUTIONS**

$$n = \frac{N}{N_A} = \frac{3.0 \times 10^{24}}{6.02 \times 10^{23}}$$

$$n = 4.98 \text{ mol}$$

$$P V = n R T$$

$$V = \frac{n R T}{P}$$

$$V = \frac{(4.98) (8.313) (300)}{1.20 \times 10^5}$$

$$V = \frac{12419.6}{1.20 \times 10^5}$$

$$V = 0.103 \text{ m}^3$$

- 8 Calculate the root mean square velocity of hydrogen molecules at  $0^\circ\text{C}$  and 1.0 atm pressure. Assuming hydrogen to be an ideal gas. Under these conditions hydrogen has a density  $\rho$  of  $8.99 \times 10^{-2} \text{ kg/m}^3$ .

**DATA**

$$T = 0^\circ\text{C}$$

$$T = 0 + 273 = 273 \text{ K}$$

$$P = 1 \text{ atm} = 1.01 \times 10^5 \text{ Pa}$$

$$\rho = 8.99 \times 10^{-2} \text{ kg/m}^3$$

$$v_{rms} = ?$$

**SOLUTIONS**

$$P = \frac{1}{3} \rho \overline{v^2}$$

$$\overline{v^2} = \frac{3 P}{\rho}$$

Taking root on both the side

$$\sqrt{\overline{v^2}} = \sqrt{\frac{3 P}{\rho}}$$

$$v_{rms} = \sqrt{\frac{3 P}{\rho}}$$

$$v_{rms} = \sqrt{\frac{3 (1.01 \times 10^5)}{8.99 \times 10^{-2}}}$$

$$v_{rms} = 1835.86 \text{ m/s}$$

- 9 Calculate the root mean square speed of hydrogen molecule at 500K (mass of proton =  $1.67 \times 10^{-27}$  kg and  $k = 1.38 \times 10^{-23}$  J/ K)

**DATA**

$$T = 500 \text{ K}$$

$$m_p = 1.67 \times 10^{-27} \text{ kg}$$

$$m_H = 2 \times 1.67 \times 10^{-27} \text{ kg}$$

$$m_H = 3.34 \times 10^{-27} \text{ kg}$$

$$k = 1.38 \times 10^{-23} \text{ J/K}$$

$$v_{rms} = ?$$

**SOLUTIONS**

$$\frac{1}{2} m_H \overline{v^2} = \frac{3}{2} k T$$

$$\overline{v^2} = \frac{3 k T}{m_H}$$

Taking root on both the side

$$\sqrt{\overline{v^2}} = \sqrt{\frac{3 k T}{m_H}}$$

$$v_{rms} = \sqrt{\frac{3 k T}{m_H}}$$

$$v_{rms} = \sqrt{\frac{3 (1.38 \times 10^{-23})(500)}{3.34 \times 10^{-27}}}$$

$$v_{rms} = 2489.49 \text{ m/s}$$

- 10 (a) Determine the average value of the Kinetic energy of the particles of an ideal gas at  $10^\circ\text{C}$  and at  $40^\circ\text{C}$ .  
 (b) What is the Kinetic energy per mole of an ideal gas at these temperatures?

**DATA**

(a)

$$T = 10^\circ\text{C} = 10 + 273 = 283 \text{ K}$$

$$T = 40^\circ\text{C} = 40 + 273 = 313 \text{ K}$$

(b)

$$\text{kinetic energy per mole} = ?$$

**SOLUTIONS**

Average K.E at  $10^\circ\text{C}$

$$(K.E)_{av} = \frac{3}{2} k T$$

$$(K.E)_{av} = \frac{3}{2} (1.38 \times 10^{-23}) (283)$$

$$(K.E)_{av} = 5.858 \times 10^{-21} \text{ J}$$

Average K.E at  $40^\circ\text{C}$

$$(K.E)_{av} = \frac{3}{2} k T$$

$$(K.E)_{av} = \frac{3}{2} (1.38 \times 10^{-23}) (313)$$

$$(K.E)_{av} = 6.479 \times 10^{-21} \text{ J}$$

Kinetic energy per mole at  $10^\circ\text{C}$

$$E = N_A (K.E)_{av}$$

$$E = (6.02 \times 10^{23}) (5.858 \times 10^{-21})$$

$$E = 3521.7 \text{ J}$$

Kinetic energy per mole at  $40^\circ\text{C}$

$$E = N_A (K.E)_{av}$$

$$E = (6.02 \times 10^{23}) (6.479 \times 10^{-21})$$

$$E = 3900.35 \text{ J}$$